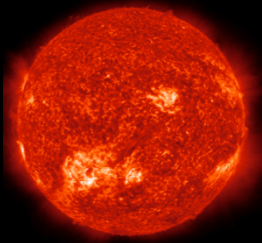


# Understanding GWs from core-collapse supernovae

Pablo Cerdá-Durán - University of Valencia



# Core collapse supernovae

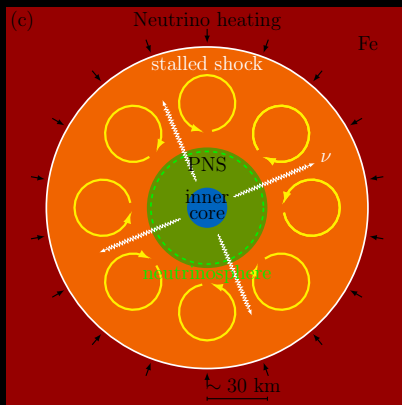


## Collapse of the core of massive stars ( $8-100 M_{\odot}$ )

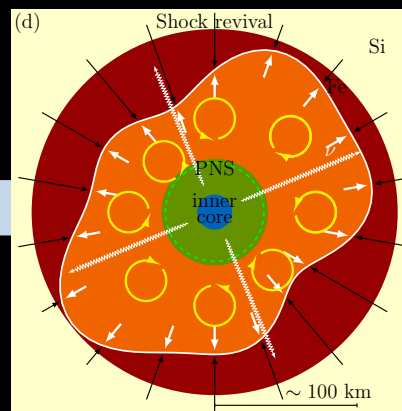
- Non-rotating progenitors ( $>99\%$ ) (Li et al 2011, Chapman et al 2007)
- Observable within  $\sim 10$  kpc (Gossan et al 2015, Powell & Müller 2018)
- Rare events ( $\sim 1/30$  year in our galaxy) (Adams et al 2013)

### 1. Collapse

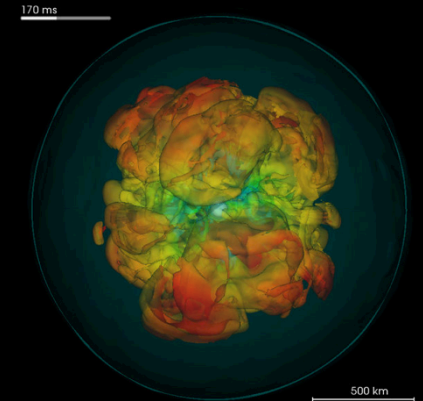
### 2. PNS formation



### 3. PNS + shock instabilities

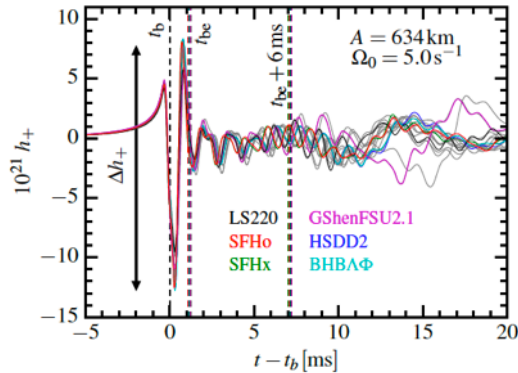


### 3. Neutrino-driven explosion



# GW signal in CCSNe: timeline

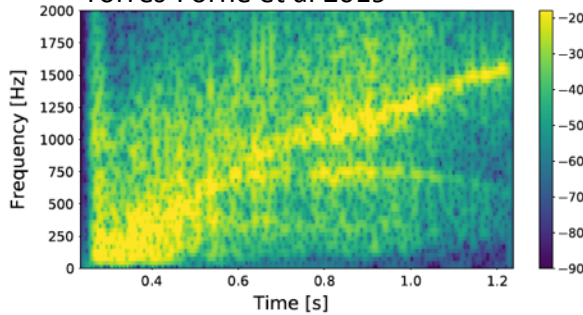
Richers et al 2017



## Bounce signal:

- only fast rotating models
- $\Delta t \sim 5 \text{ ms}$
- $f \sim 600\text{-}900 \text{ Hz}$
- $h \sim 10^{-21}$  @ 10 kpc

Torres-Forné et al 2019



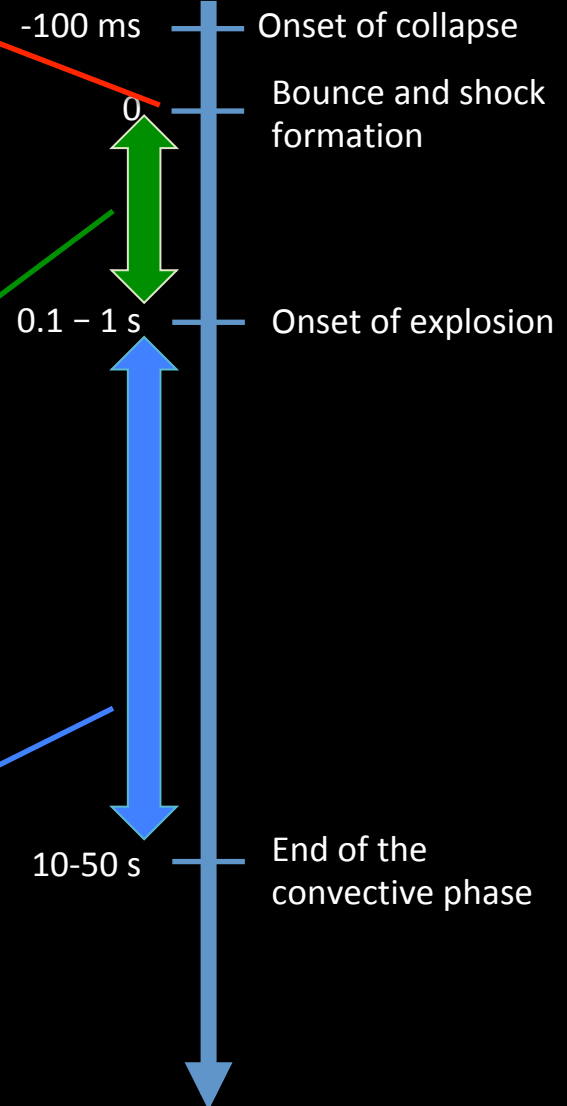
## Post-bounce “SN” signal:

- g-modes, SASI, convection
- $\Delta t \sim 0.1\text{-}1\text{-s}$
- $f \sim 50\text{-}2000 \text{ Hz}$
- $h \sim 10^{-23}\text{-}10^{-22}$  @ 10 kpc



## PNS convection signal:

- Computationally expensive
- $\Delta t \sim 10\text{-}50\text{-s}$
- $f \sim ?$
- $h \sim ?$



# Post –bounce signal

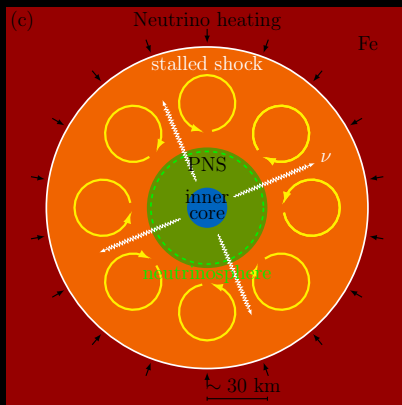
## PNS phase (before explosion):

- Duration:  $\sim 0.1 - 1$  s
- PNS mass grows:  $\sim 0.5 M_{\odot} \rightarrow 1.4 - 2 M_{\odot}$
- PNS shrinks:  $\sim 30$  km  $\rightarrow \sim 10$  km
- PNS cools down

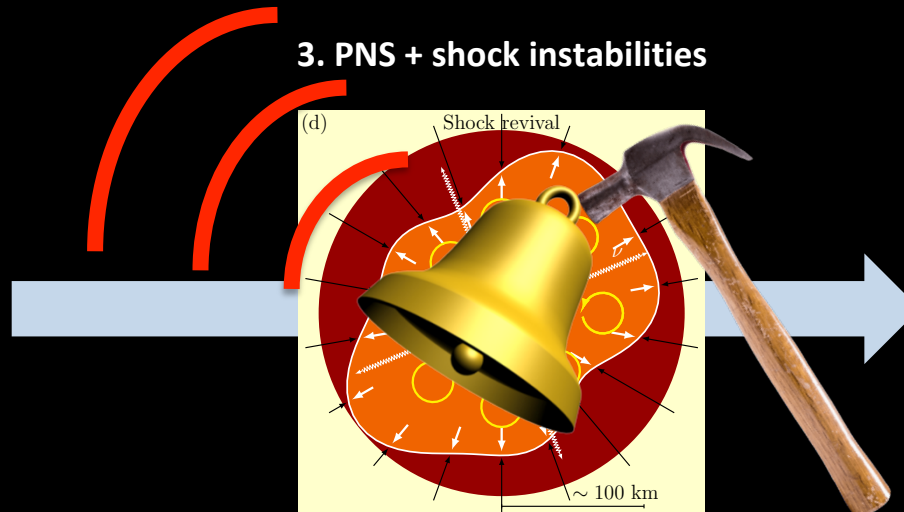
## PNS excitation

- The “hammer”: convection, SASI
- The “bell”: proto-neutron star
- The “ring”: PNS normal modes

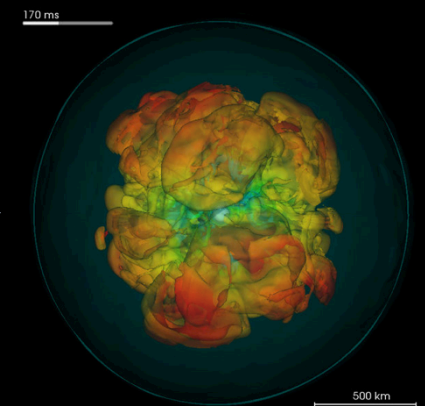
### 2. PNS formation



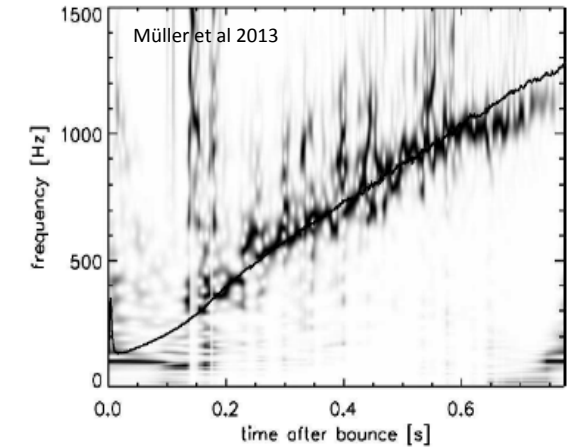
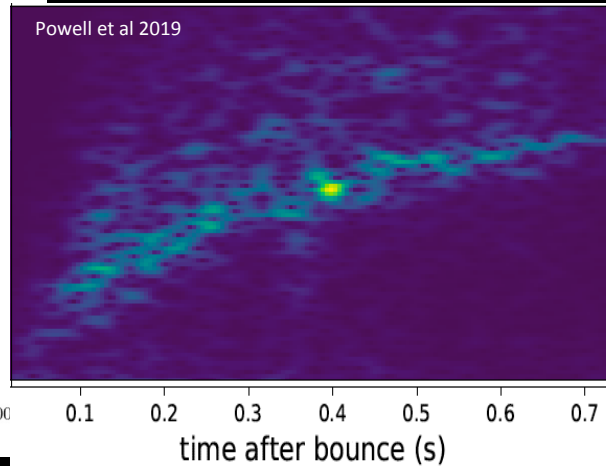
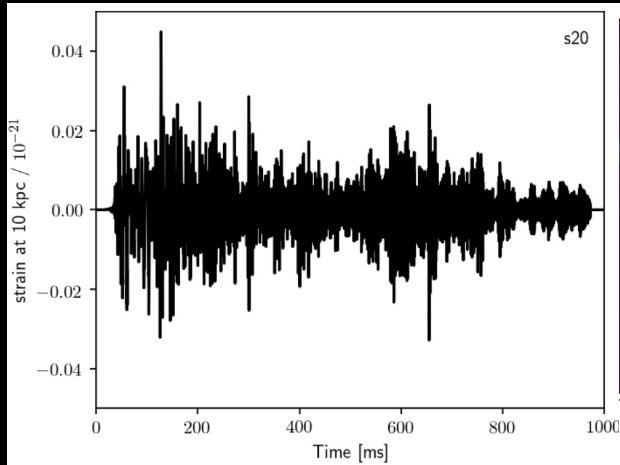
### 3. PNS + shock instabilities



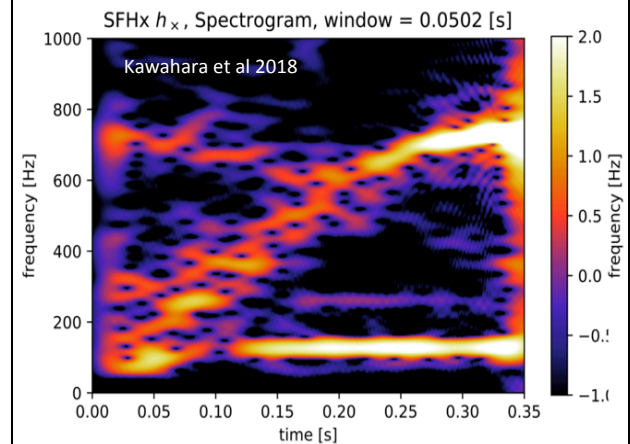
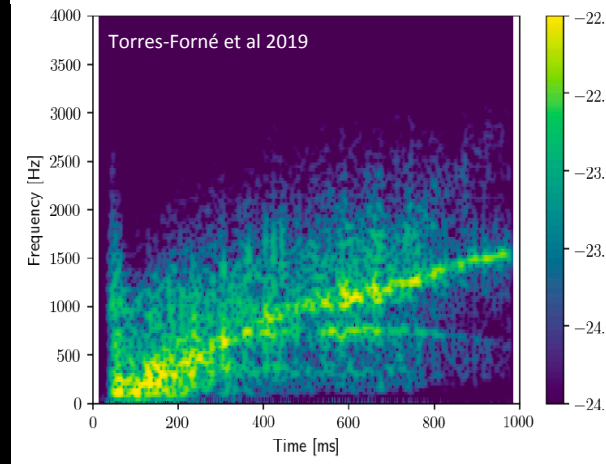
### 3. Neutrino-driven explosion



# GW emission from PNS oscillations



- Highly stochastic
- Time evolving frequencies (g-modes, SASI)



**What information can we extract from these modes?**

# PNS asteroseismology

- Which modes can be observed?



Mode identification

- How do mode frequencies depend of PNS properties?

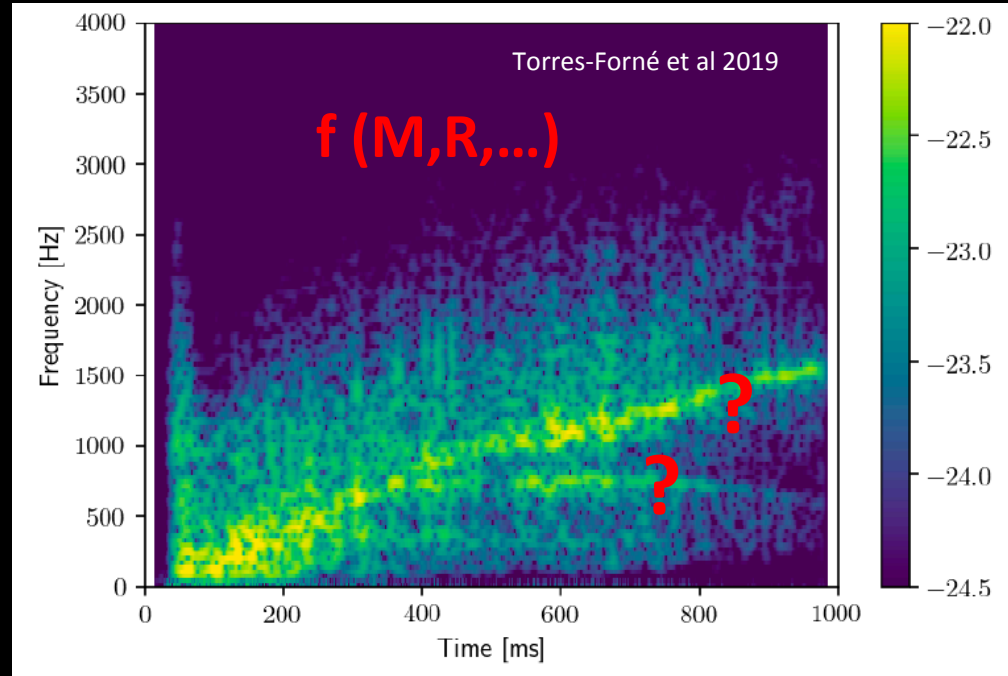


Universal relations

- Can we extract this information from the detectors noise?



Inference



# Mode identification

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## Collaborators:

- A. Torres-Forné, M. Obergaulinger, J. A. Font (U. Valencia)
- A. Passamonti

## Publications:

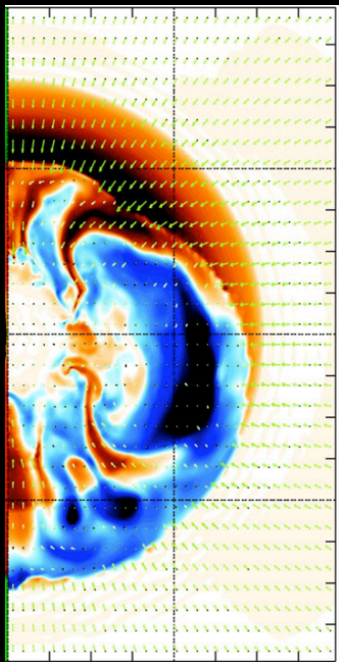
- Torres-Forné et al 2018 (arXiv: 1806.11366)
- Torres-Forné et al 2019a (arXiv: 1708.01920)



# PNS oscillations

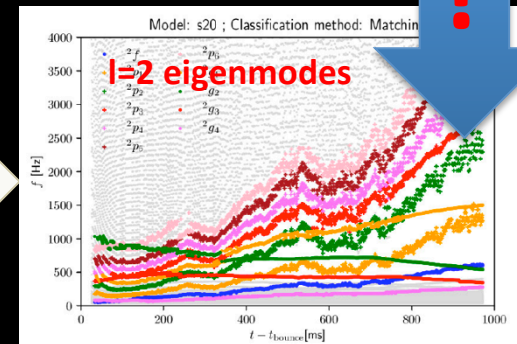
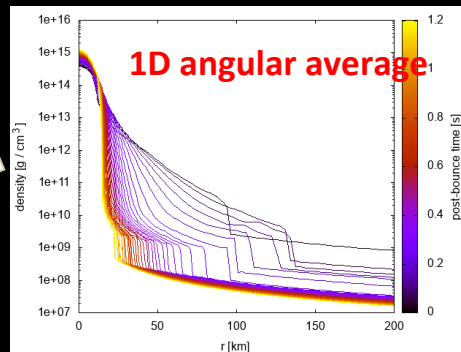
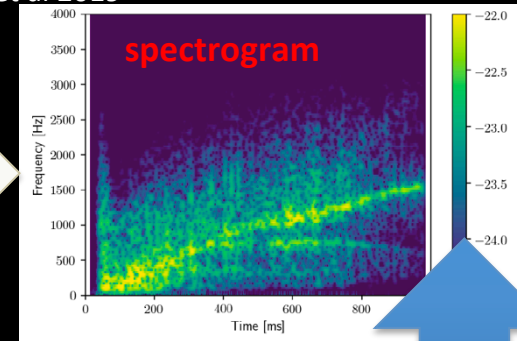
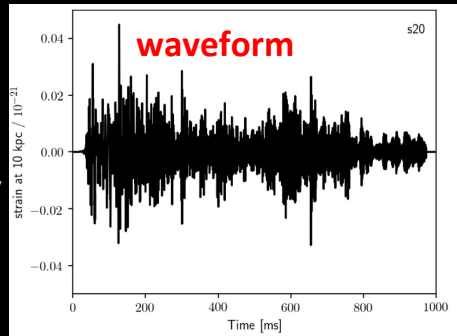
Analysis of GW signal from simulation

Multi-dimensional  
numerical simulation



Obergaulinger et al 2013

Torres-Forné et al 2019



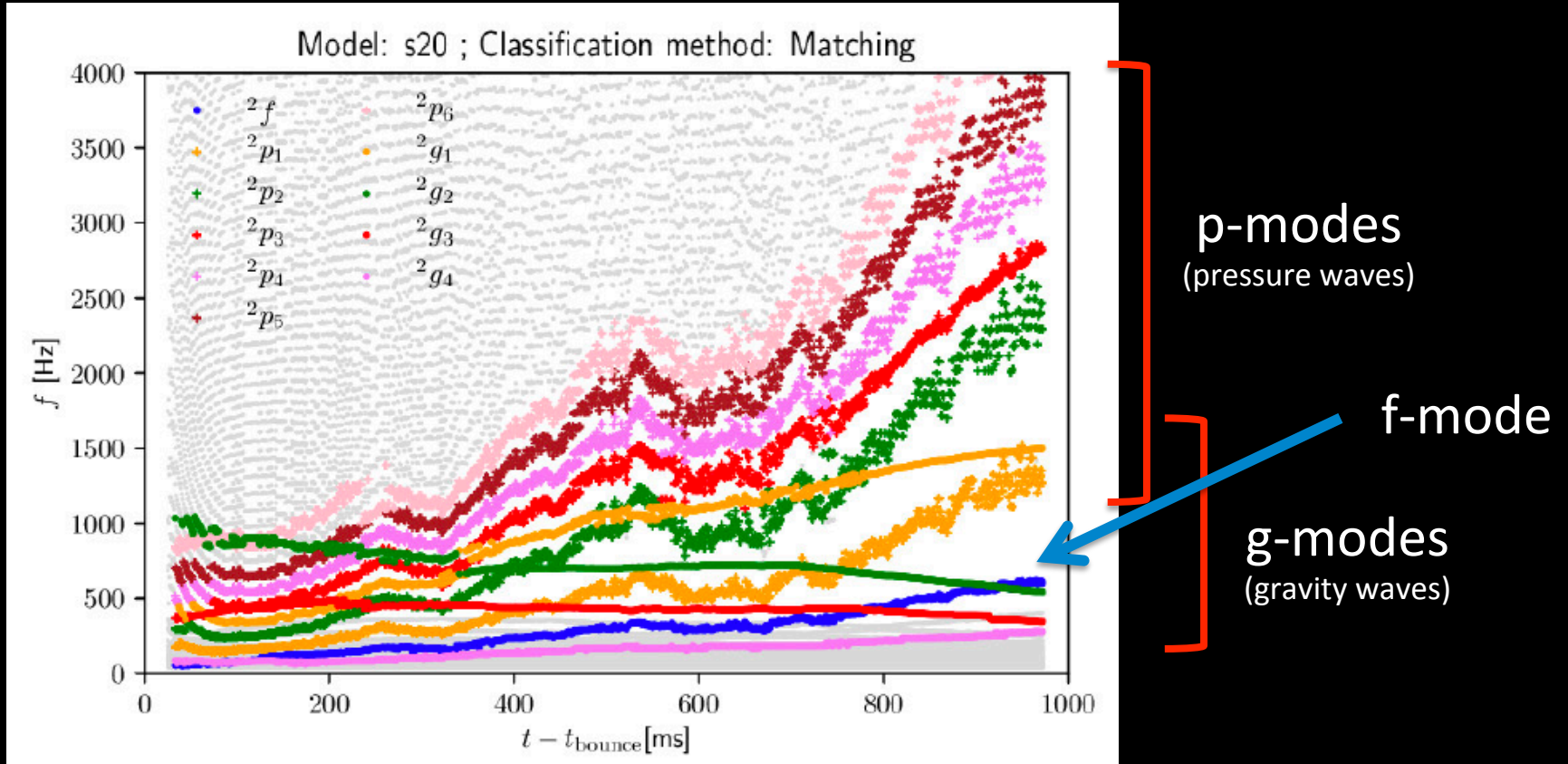
Torres-Forné et al 2018

Linear perturbation analysis of 1d background



# Classified modes

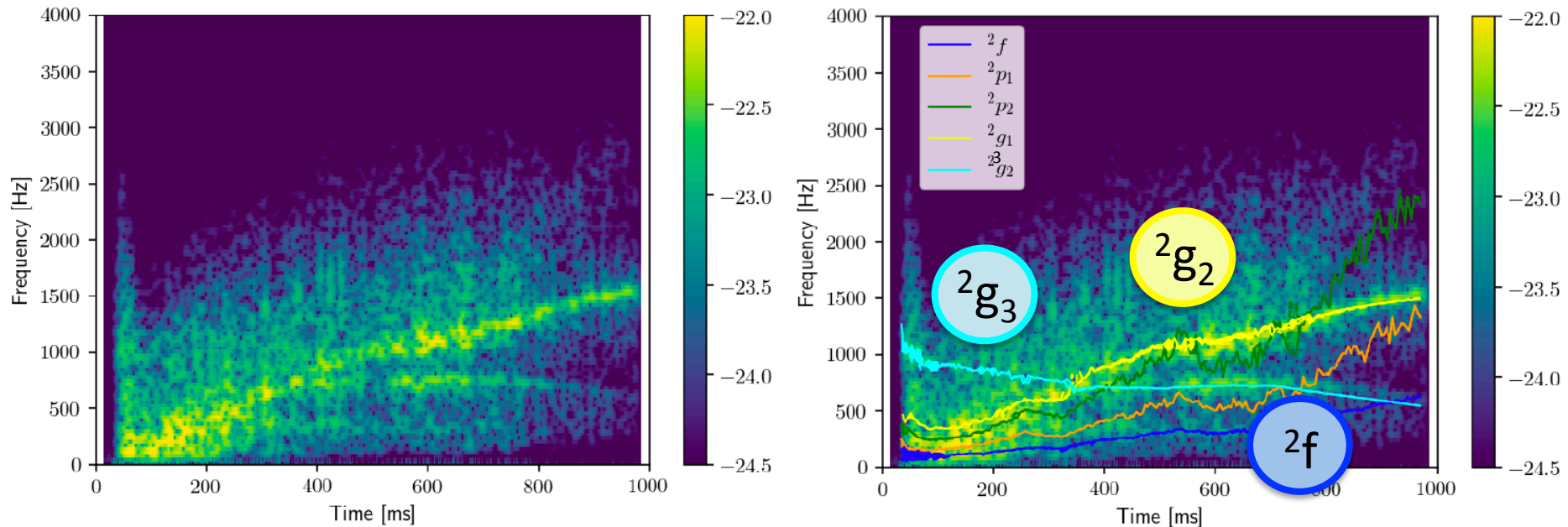
Computed using GREAT (General Relativistic Eigenmode Analysis Tool)



Torres-Forné et al 2018b

s20, SFHo EOS

# Comparison with GWs



**The main feature in all CCSN simulations is related to the excitation of a particular g-mode ( $2g_2$  in our notation)**

# Universal relations

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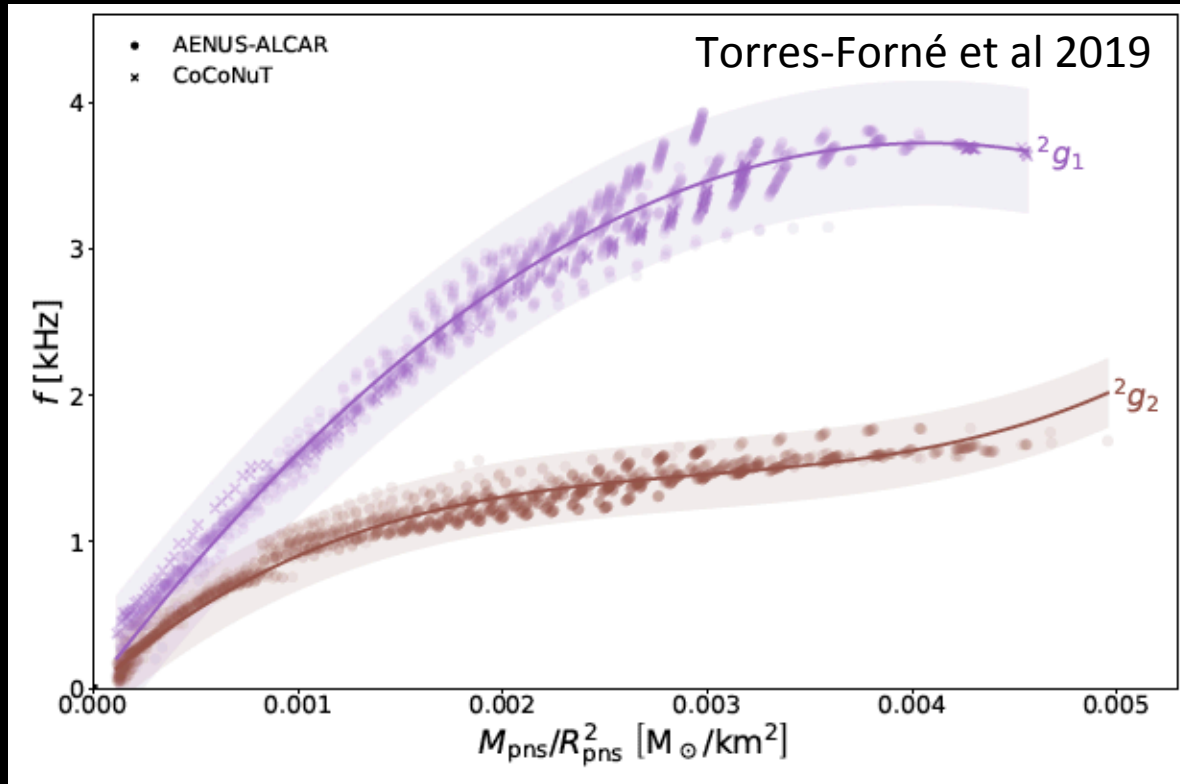
Collaborators:

- A. Torres-Forné, M. Obergaulinger, J. A. Font (University of Valencia)
- B. Müller (Monash University)

Publications:

- Torres-Forné et al 2019b (arXiv: 1902.10048)

# Universal relations: g-modes



- 26 1D simulations
- 2 codes
  - Alcar-Aenus
  - CoCoNuT
- 6 EOS:
  - LS220
  - Gshen-NL3
  - Hshen
  - SFHo
  - BHB- $\Lambda$
  - Hshen- $\Lambda$
- 8 progenitors (11.2 – 75  $M_{\odot}$ )

$$f({}^2g_2) = b x + c x^2 + d x^3$$

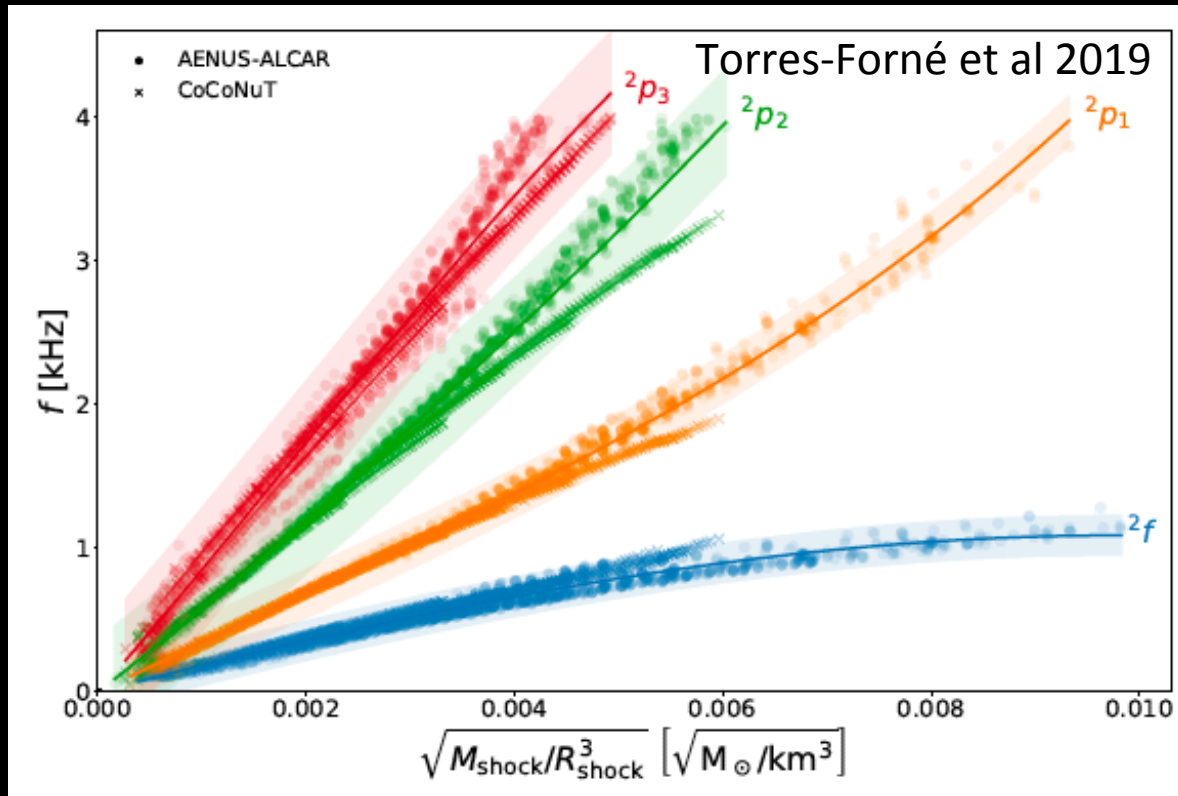
$$x = M_{\text{PNS}}/R_{\text{PNS}}^2$$

**g-modes scale with PNS surface gravity**

**No dependence on EOS**

PNS definition:  $\rho > 10^{11} \text{ g/cm}^3$

# Universal relations: f and p-modes



$$f \text{ (} {}^2f \text{)} = b x + c x^2$$

$$x^2 = M_{\text{shock}}/R_{\text{shock}}^3$$

**f and p-modes scale with sqrt. of mean density inside the shock**

**Their frequency traces (mainly) the location of the shock**

# Inference

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## Collaborators:

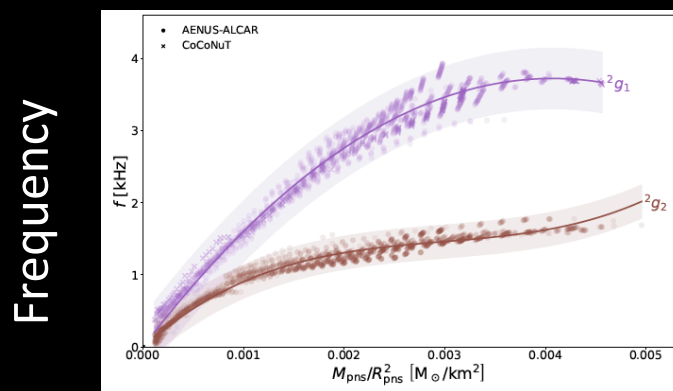
- A. Torres-Forné, M. Obergaulinger, J. A. Font (University of Valencia)
- M.A. Bizouard, N. Christensen (Observatoire Côte d'Azur)
- P. Maturana, R. Meyer (University of Auckland)

## Publications:

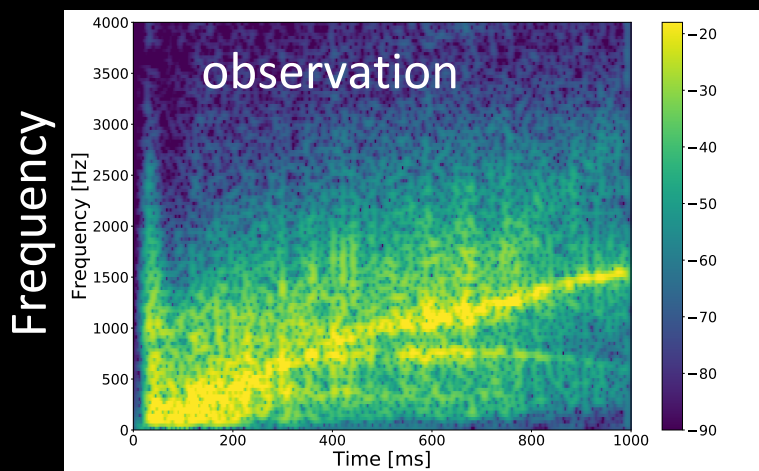
- Bizouard et al 2020 (arXiv: 2012.00846)

# Inference (inverse problem)

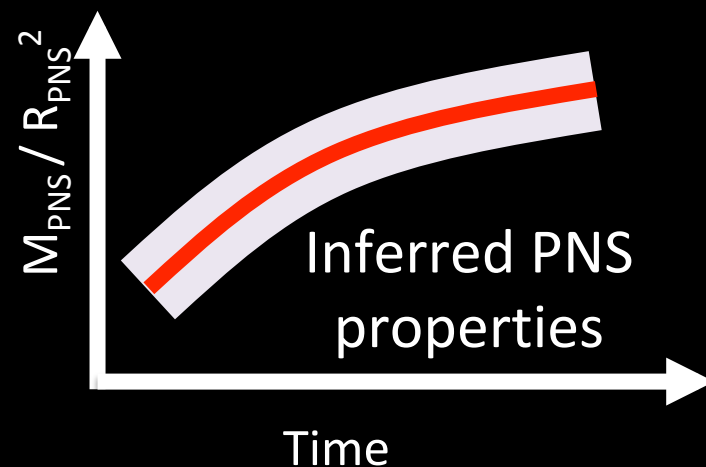
Universal relations



$$M_{\text{PNS}} / R_{\text{PNS}}^2$$

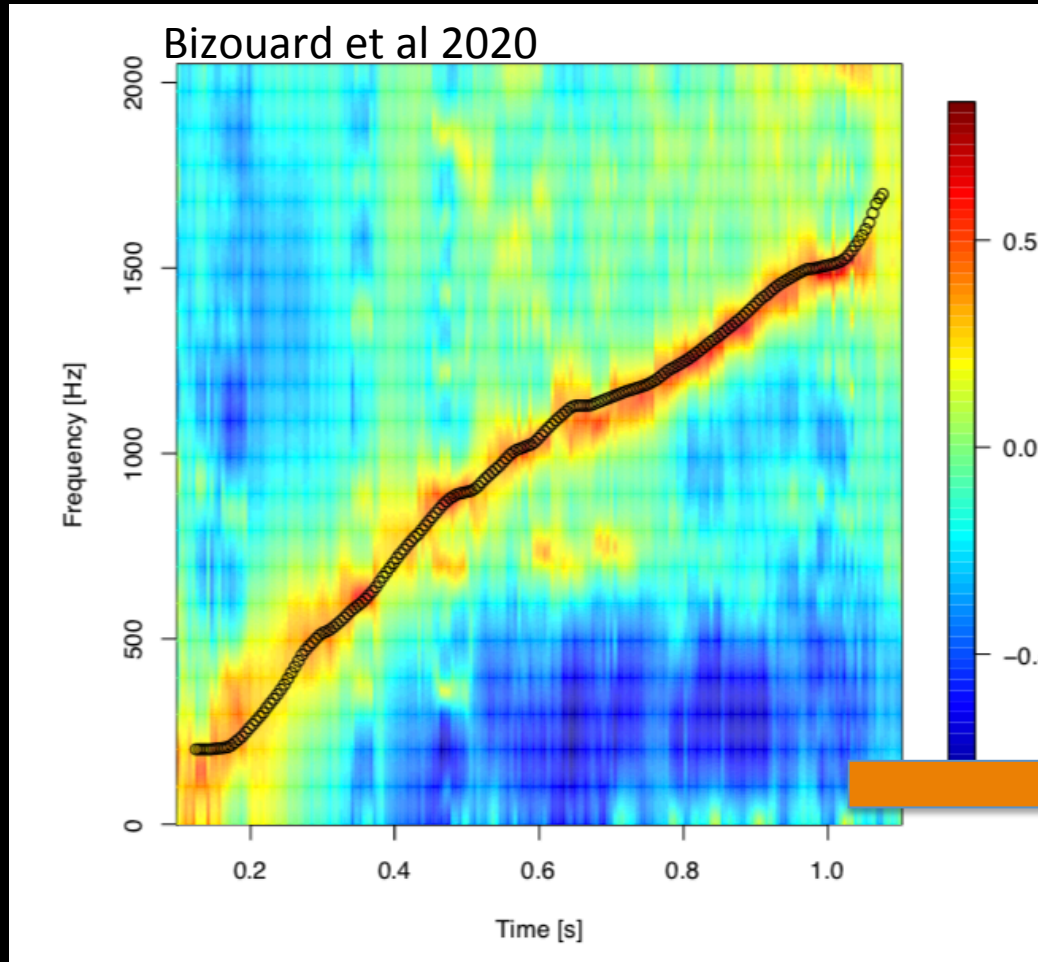


Time





# Mode extraction



Test GW data:

- Simulations: 8 x 2D
- Code: Aenus-Alcar
- Progenitors: 11.2-40  $M_{\odot}$
- EOS: LS220 and Gshen

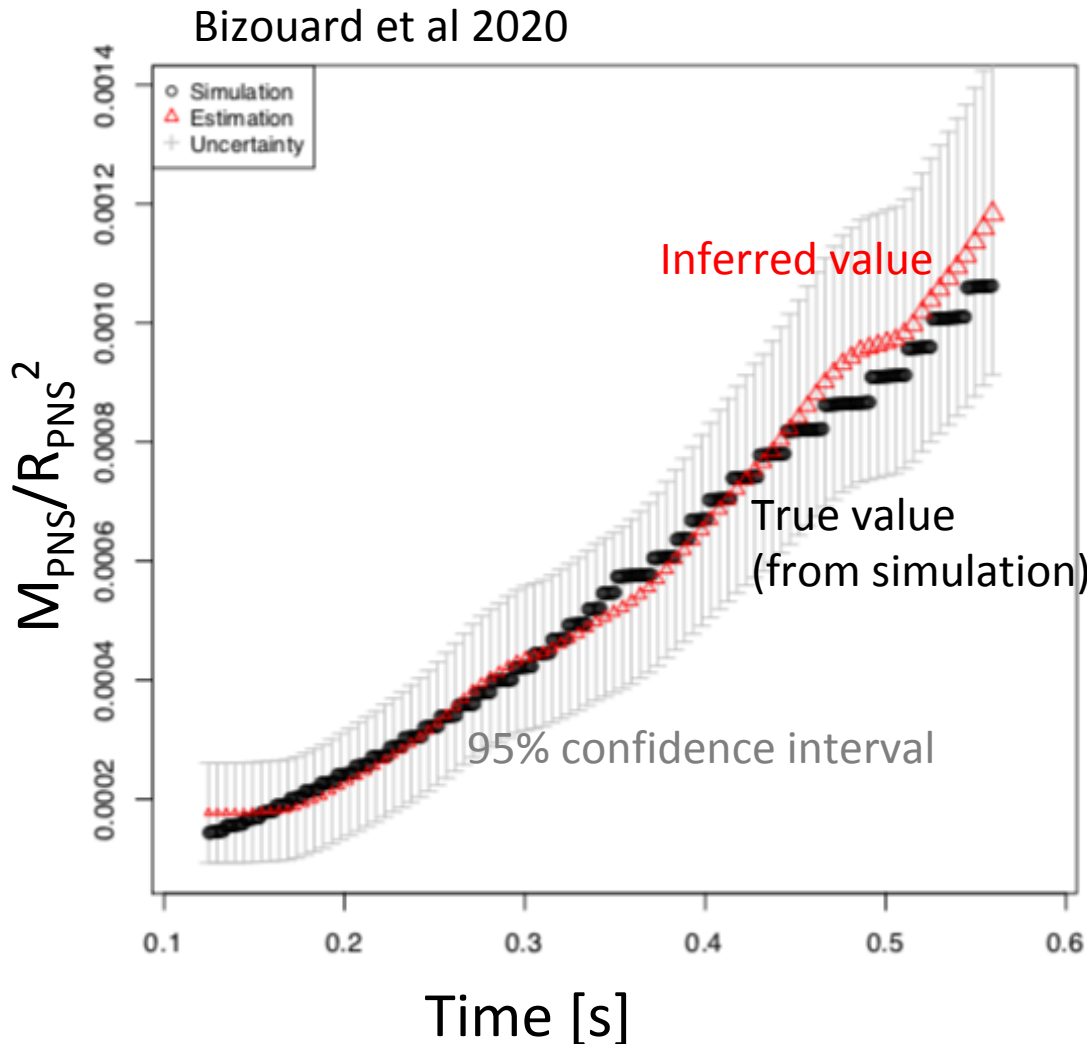
Injectons in detector noise:

- Single detector: aLIGO, aVirgo, ET or CE.
- Gaussian colored noise

Time-frequency tracking  
of the main ridge

$$f(t)$$

# Inference of surface gravity



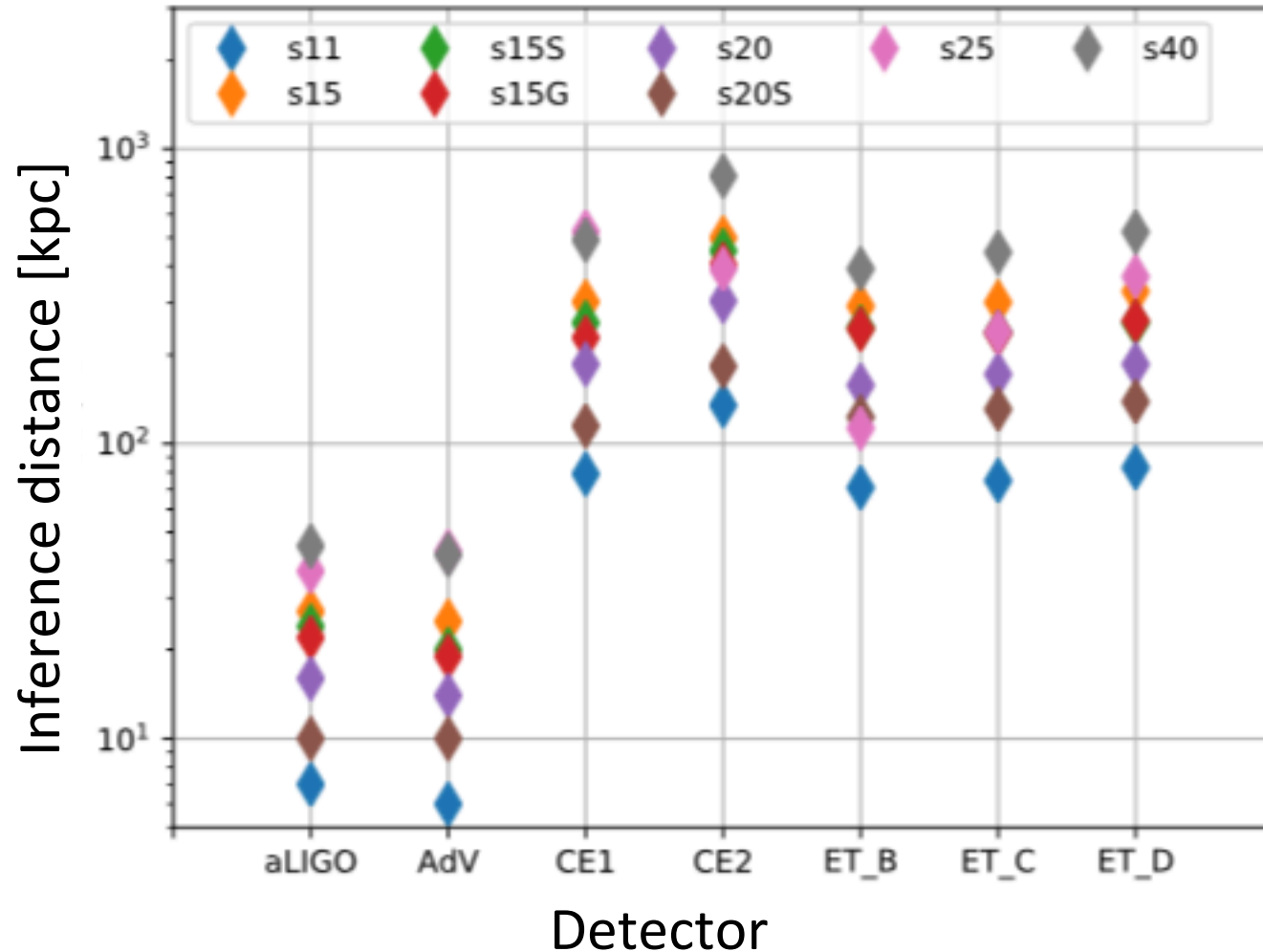
For sufficiently close sources we can measure the surface gravity only from GW data

Errors estimated using the dispersion in the universal relations (do not include errors due to detector's noise)

The inference is as good as the model: Alcar-Aenus was used for both the 2D simulations and to build the universal relations (1D simulations).

# Inference distance

Bizouard et al 2020



# Inference from the bounce signal

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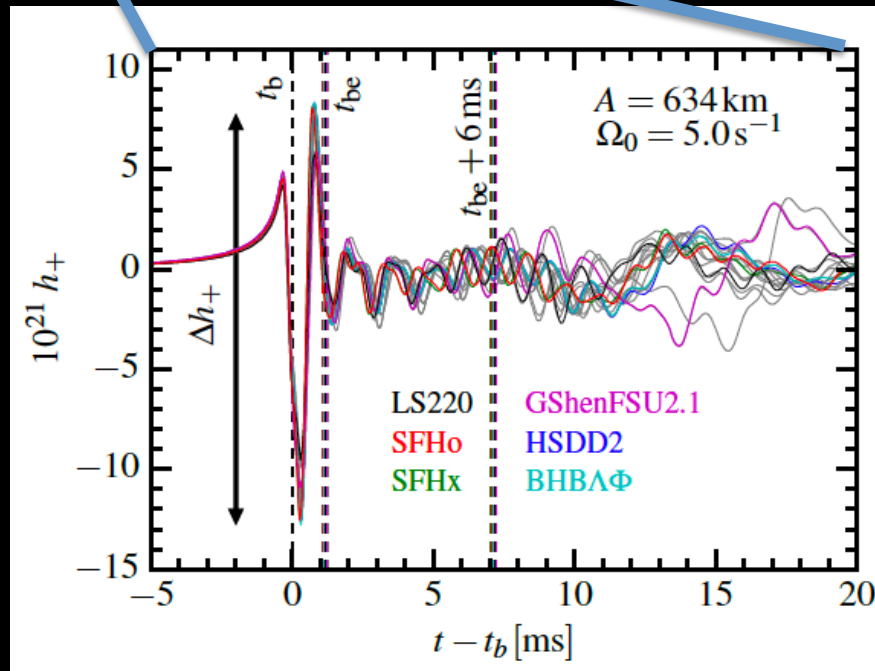
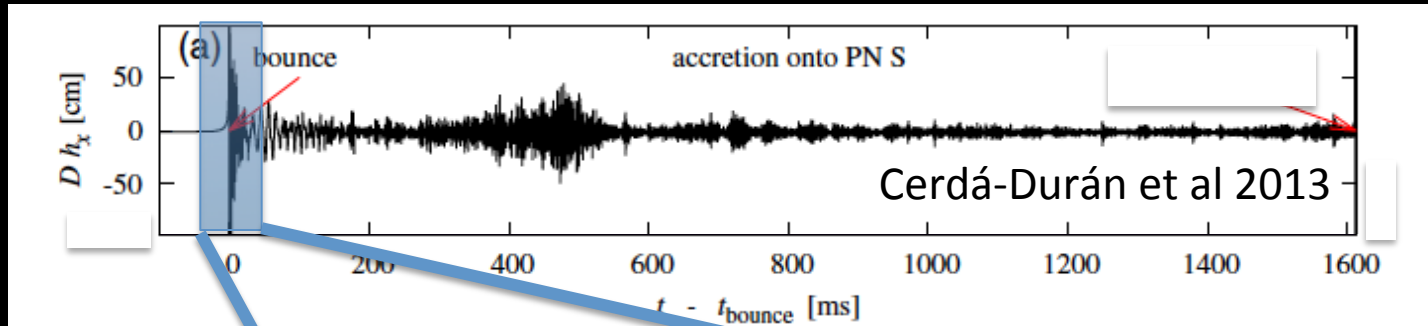
## Collaborators:

- C. Pastor-Marcos (University of Valencia / University of Heiledberg)
- A. Torres-Forné, J. A. Font (University of Valencia)
- E. Abdikamalov (Nazarbayev University)
- S. Richers (UC Berkeley)

## Publications:

- Pastor-Marcos et al (in preparation)

# Bounce GW signal

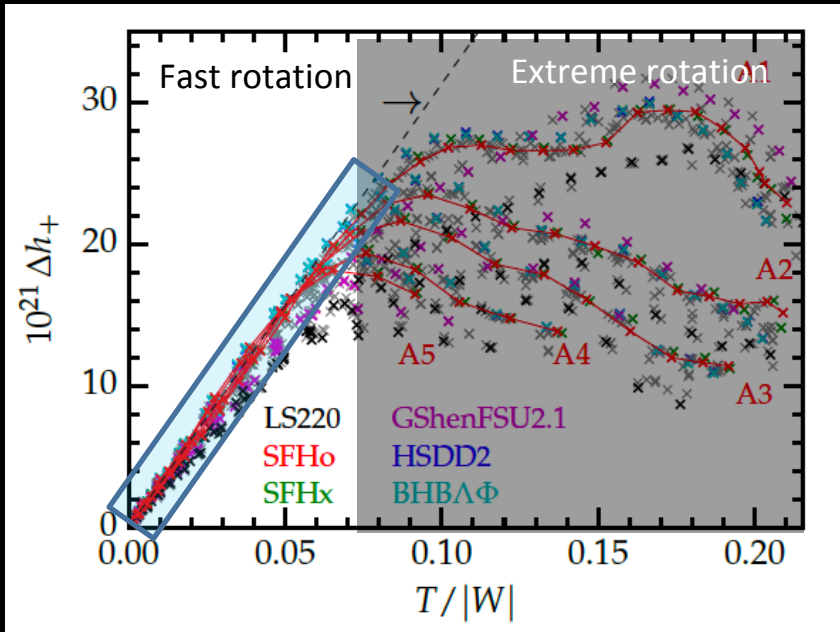


Richers et al 2017

- Only first few ms
- Only rotating models (zero for non-rotating): <1% SNe
- Main features:
  - Peak with amplitude  $\Delta h_+$
  - Several oscillations with frequency  $f_{\text{peak}}$
- Richers et al catalogue
  - 2D GR simulations
  - 1824 waveforms
  - 18 different EOS

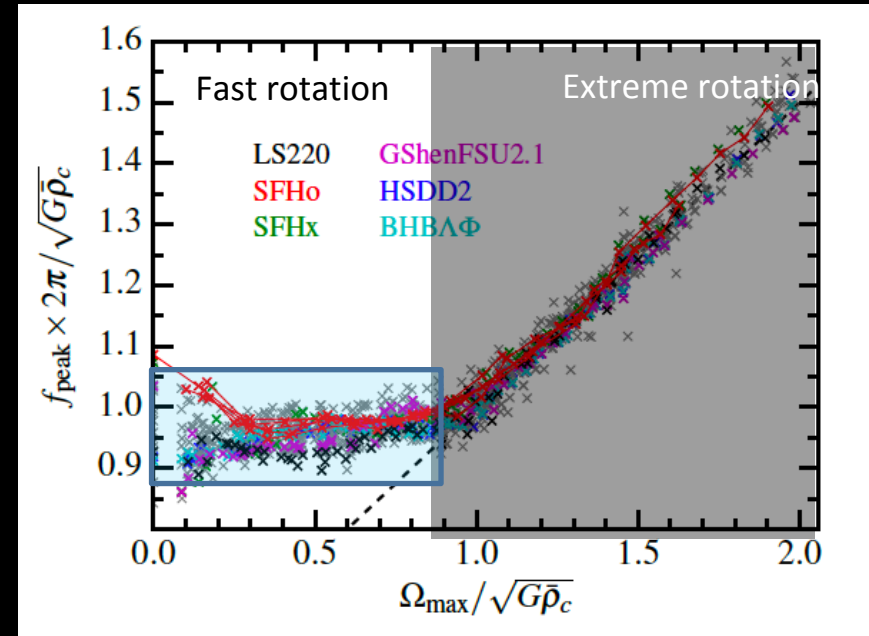
# What can we learn from $\Delta h_+$ and $f_{\text{peak}}$ ?

Richers et al 2017



$$\Delta h_+ \propto T / |W|$$

Kinetic rotational to potential energy ratio  
(measure of rotation)

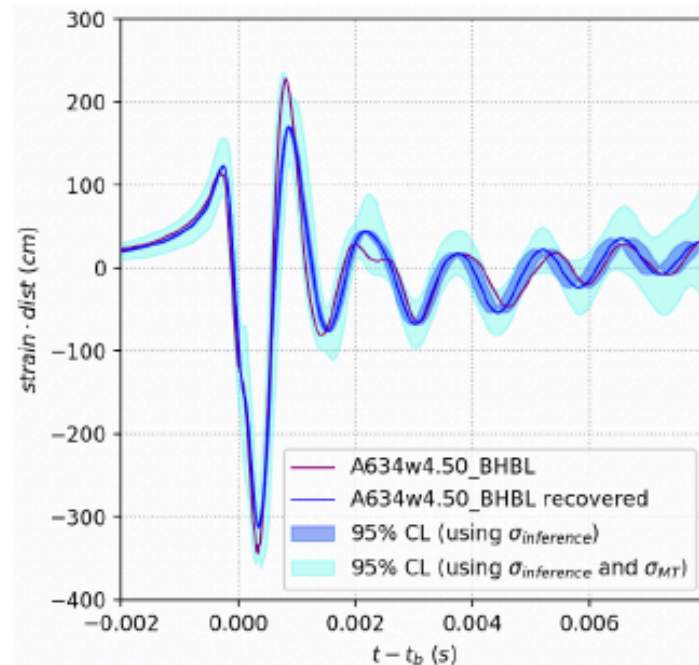
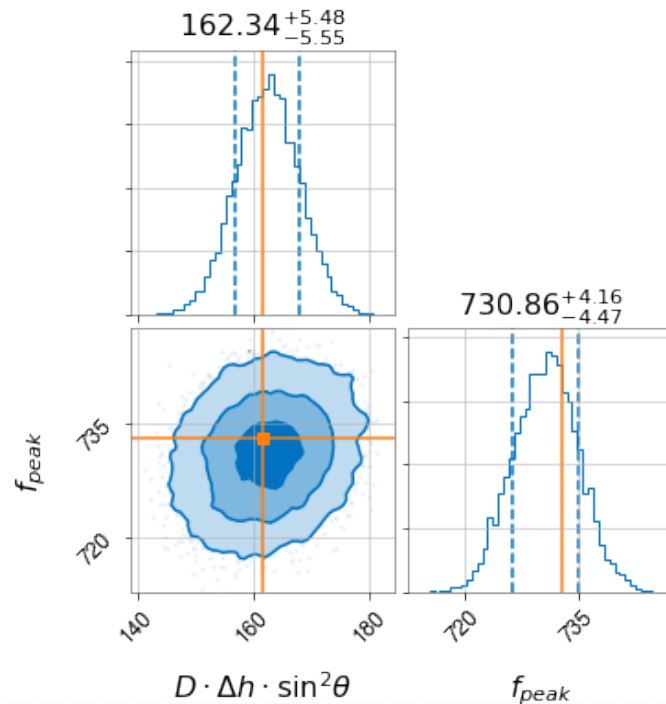


$$f_{\text{peak}} \propto \sqrt{\rho_c}$$

Central density

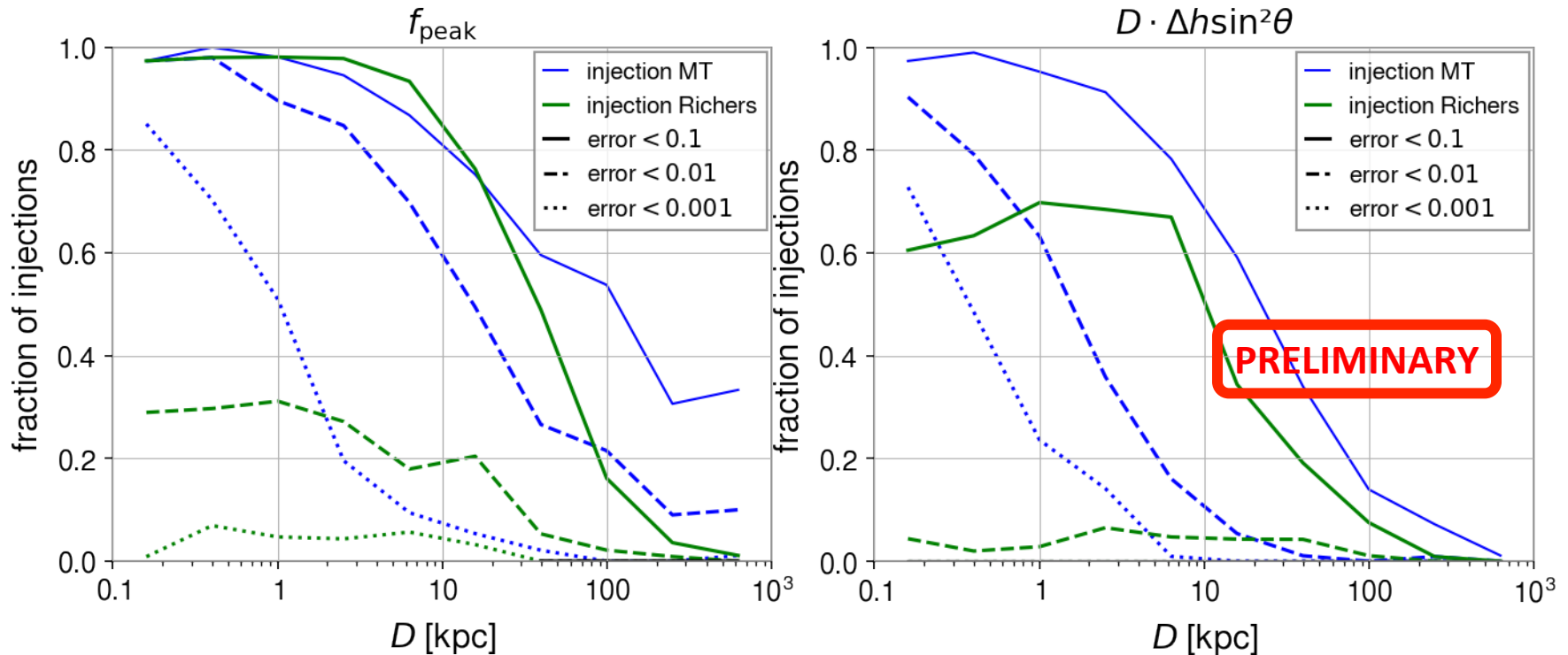
# Bayesian inference with

- Injections in Gaussian colored noise
- 3 detector network (2 x aLigo + aVirgo)
- 1000 random injections in the sky with  $D = [0.1, 1000]$  kpc





# Inference distance



- Inference with  $\sim 10\%$  errors is possible within 10-50 kpc (only fast rotating progenitors)
- Value of  $\Delta h$  is degenerated with inclination angle

# GWs from the long term evolution of a PNS

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Collaborators:

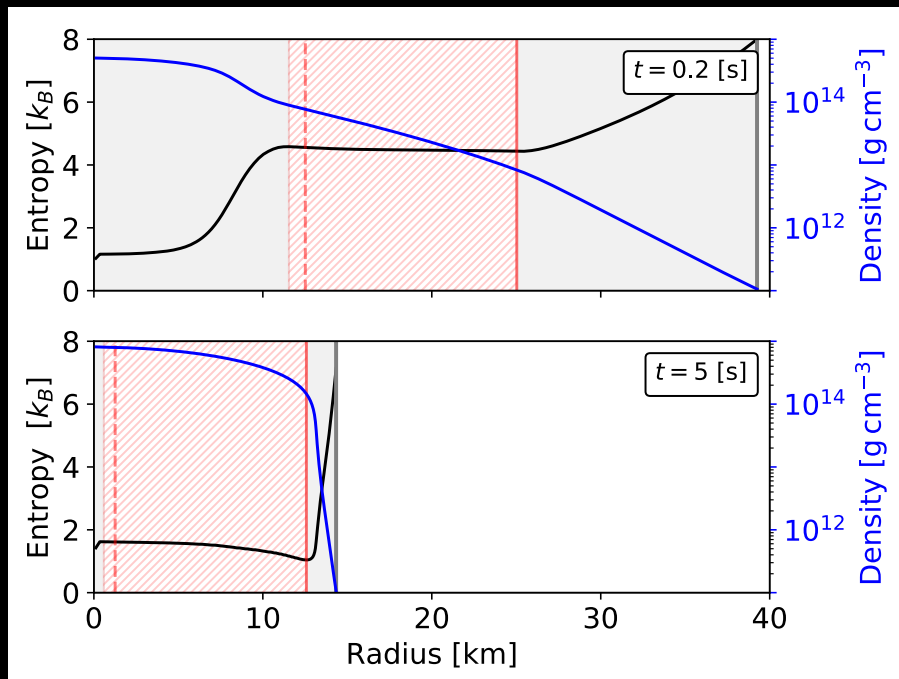
- R. Raynaud, J. Guilet (CEA-Saclay)

Publications:

- Raynaud et al (in preparation)

# Long term evolution of the PNS ( $>1$ s)

- MHD 3D simulations in the anelastic approximation (sound waves filtered)
- MagIC pseudo-spectral code ([magic-sph.github.io](https://github.com/magic-sph))
- Recent application to proto-neutron star dynamos (Raynaud et al 2020)



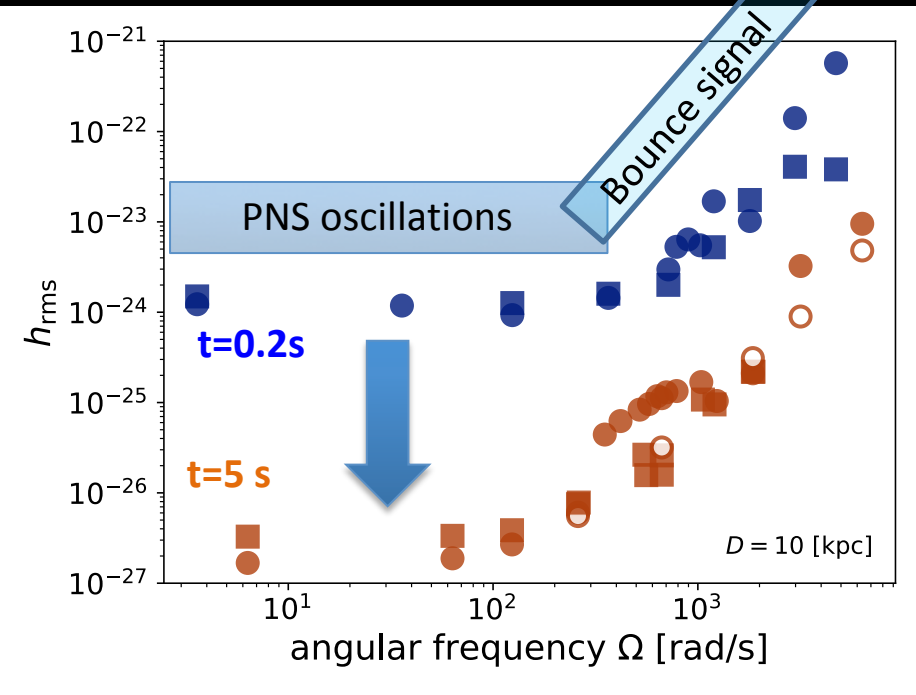
## 1. 1D background simulation:

- 7 s post-bounce
- PROMETHEOS-VERTEX code
- Energy-dependent 3-neutrino flavour transport
- Progenitor: s27.0 of Woosley et al 2002
- EOS: LS220

## 2. 3D simulation of the convection zone

- Density and temperature of the background model at 0.2 and 5 s
- Simple gray neutrino transport: constant flux at the base of the convection zone.

# Gravitational wave amplitude

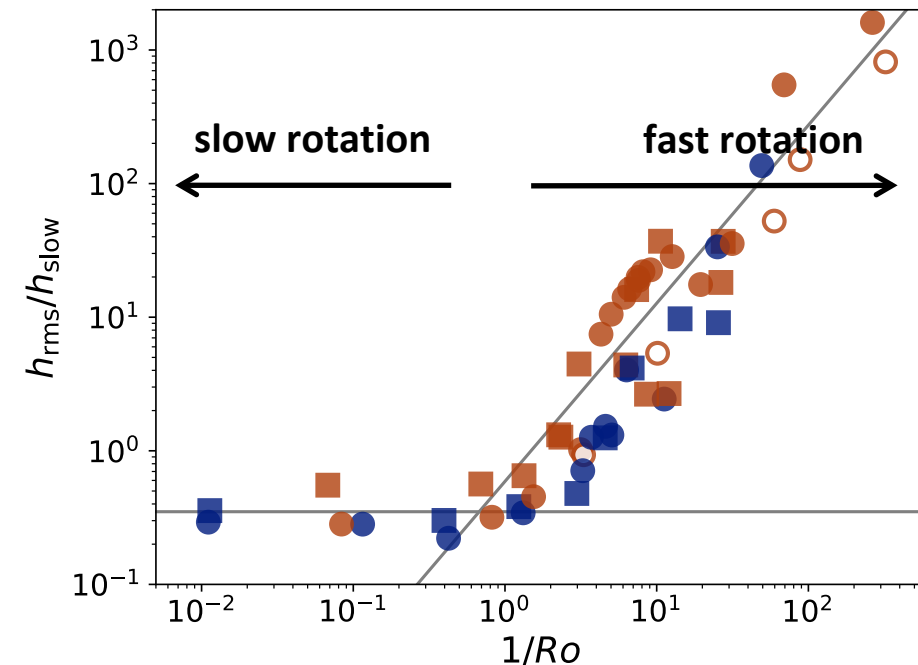


Convection decays with time rapidly in a time-scale of seconds

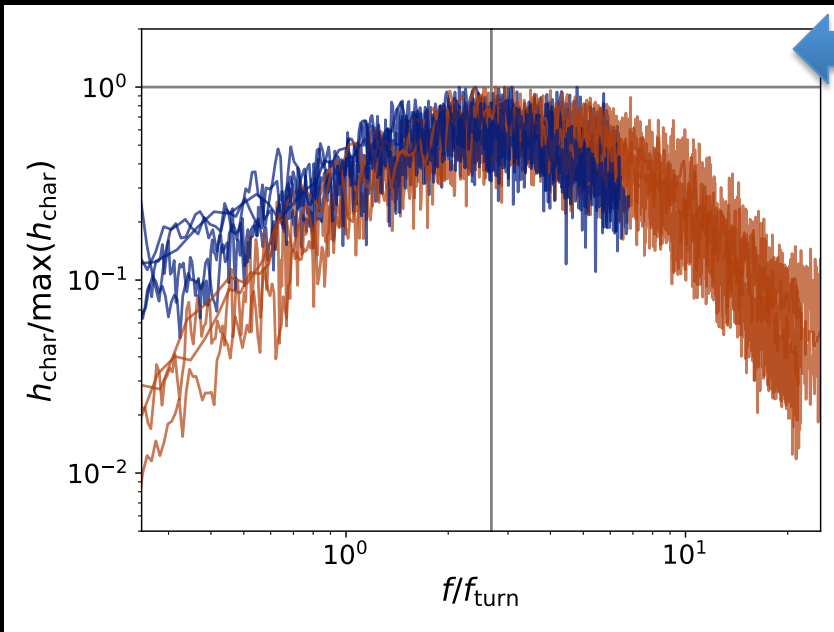
Decay can be modelled with simple scaling relations in two limits:

- Slow rotation ( $Ro \gg 1$ )
- Fast rotation ( $Ro \ll 1$ )

$$Ro = f_{\text{turn}} / f_{\text{rotation}} \rightarrow \text{Rossby number}$$



# GW frequency



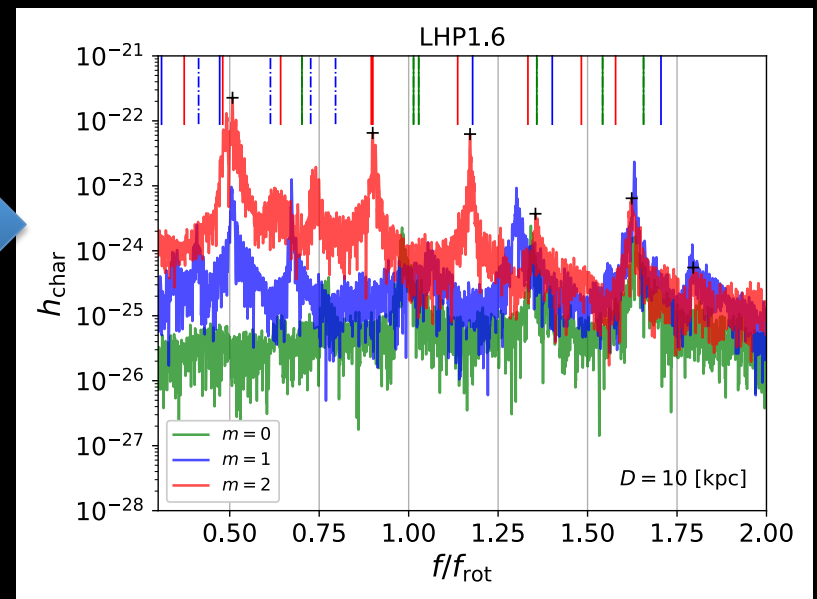
Slow rotation ( $Ro > 1$ )

Broad spectrum due to convection

Peak frequency scales with overturn (convection) frequency

Fast rotation ( $Ro < 1$ )

- Appearance of inertial modes
- GW frequency scales with rotation frequency.



# Conclusions

- GW signals offer multiple possibilities to infer properties of the PNS
  - g-modes and p-modes
  - peak frequency at bounce (only fast rotation)
  - inertial modes (only fast rotation)
- The observation of these features would confirm the CCSN model
- It is unclear which kind of information about the hot EOS could be extracted (none? Edwan et al 2021)